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JANUARY, 1913

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# THE AMERICAN MATHEMATICAL MONTHLY

FOUNDED BY BENJAMIN F. FINKEL

A JOURNAL FOR TEACHERS OF MATHEMATICS IN THE  
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CONTROLLED AND EDITED BY

C. H. ASHTON	W. DEW. CAIRNS	E. R. HEDRICK
R. P. BAKER	FLORIAN CAJORI	L. C. KARPINSKI
W. C. BRENKE	R. D. CARMICHAEL	G. A. MILLER
W. H. BUSSEY	B. F. FINKEL	H. E. SLAUGHT

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EDITORIAL COMMITTEE: H. E. SLAUGHT, G. A. MILLER, E. R. HEDRICK

EXECUTIVE COMMITTEE: H. E. SLAUGHT, W. C. BRENKE, R. D. CARMICHAEL

OFFICIAL CORRESPONDENCE should be addressed to the MANAGING EDITOR,  
H. E. SLAUGHT, 5548 Monroe Avenue, Chicago, Ill.

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## ANNOUNCEMENT

With this issue the AMERICAN MATHEMATICAL MONTHLY passes into the control of an Editorial Board consisting of representatives of eleven supporting institutions, together with B. F. FINKEL, founder of the MONTHLY and editor since its inception in 1894.

It will be the editorial policy of the MONTHLY to appeal especially to teachers of mathematics in the collegiate and advanced secondary fields, not only for the purpose of directing attention to questions of improvement in teaching in these fields, but also to foster the development of the scientific spirit among large numbers who are not now reached by the more technical journals. The MONTHLY will continue to publish original articles, but increased attention will be given to pedagogical and historical questions of interest and value to teachers of collegiate mathematics.

The constituency of such a journal should include:

- 1) All teachers of the advanced courses in secondary schools, especially those which offer trigonometry, college algebra, and analytic geometry.
- 2) All teachers of undergraduate courses in mathematics in colleges, universities, and engineering schools.
- 3) University professors of mathematics who wish to keep in touch with pedagogical movements in the collegiate field.
- 4) Graduate students in mathematics who wish to profit by historical and pedagogical discussions among teachers of experience.
- 5) All productive workers in mathematics who may occasionally desire a place of publication for articles of minimum technical difficulty suitable for the promotion of scientific interest among the average mathematical readers.
- 6) All who are interested in the proposal and solution of problems, especially those who seek assistance from co-workers with respect to actual difficulties encountered in the prosecution of research.

The need of a standard journal with such aims, in a field otherwise unoccupied in this country, will not be questioned. But its ultimate success will depend upon its speedily becoming self-supporting. This can happen only if the individuals who should form its constituency become subscribers in large numbers. In order to make this possible the subscription price will remain only \$2.00 per year *in advance*.

This copy of the MONTHLY is sent to all present subscribers, and also to a selected list of persons who, it is believed, will desire to become subscribers. The mailing list for the February issue will consist of those whose subscriptions, or renewals, are received by the Treasurer before the February number goes to press.

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## ORGANIZATION OF THE EDITORIAL BOARD

The Board of Editors of the MONTHLY is organized under Articles of Agreement in accordance with which the officers and the editorial and executive committees are elected by majority vote of all the members, the other committees being selected by the managing editor.

The names of the officers and committee members are given in this issue in the various departments, and they are here collected for convenient reference.

*Managing Editor:* H. E. SLAUGHT.

*Treasurer:* B. F. FINKEL.

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*Committee on Notes and News:* FLORIAN CAJORI, W. H. BUSSEY, W. DEW. CAIRNS, G. A. MILLER.

The members of these committees will welcome suggestions and criticisms from all sources, especially from those who are interested in helping the MONTHLY to realize its ideals.

The regular edition of the MONTHLY, as at present planned, is to contain thirty-two pages and cover. The present number is somewhat larger.

It is intended to go to press on the fifteenth of the month, as nearly as possible. The delay in this issue was unavoidable on account of the many adjustments incident to the reorganization.

The annual volume will consist of ten numbers, none being issued in the months of July and August.